

Parametric Equations

Convert the following parametric equations to cartesian form. Sketch and indicate orientation.

$$1. \ x = 1 - t, \ y = \frac{t}{1-t}$$

$$t = 1 - x$$

$$y = \frac{1-x}{-x}$$

$$2. \ x = 2 - \cos t, \ y = 3 \sin t + 1$$

$$\cos t = 2 - x$$

$$t = \arcsin(2 - x)$$

$$y = 3 \sin(2 - x) + 1$$

$$3. \ x = \sqrt{t}, \ y = 2t + 4$$

$$t = x^2$$

$$y = 2x^2 + 4, \ x \geq 0$$

$$4. \ x = \arctan t, \ y = 1 + t^2 \text{ or } t^2 - 1$$

$$t = \tan x$$

$$y = 1 + \tan^2 x \Rightarrow y = \sec^2 x, \ -\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$$

$$5. \ x = 2 - \frac{1}{t}, \ y = 2t + \frac{1}{t}$$

$$\frac{1}{t} = 2 - x \Rightarrow t = \frac{1}{2-x}$$

$$y = \frac{2}{2-x} + 2 - x$$

$$6. \ x = 1 + \frac{1}{t}, \ y = t - 1$$

$$\frac{1}{t} = x - 1 \Rightarrow t = \frac{1}{x-1}$$

$$y = \frac{1}{x-1} - 1$$

$$y = \frac{1}{x-1} - \frac{x-1}{x-1}$$

$$y = \frac{2-x}{x-1}$$

$$7. \ x = \cos 2\theta, \ y = \sin \theta$$